

Formulas from Trigonometry

$$\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{y}{r}$$

$$\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{x}{r}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{y}{x} = \frac{\sin \theta}{\cos \theta}$$

$$\csc \theta = \frac{\text{hyp}}{\text{opp}} = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{\text{hyp}}{\text{adj}} = \frac{1}{\cos \theta}$$

$$\cot \theta = \frac{\text{adj}}{\text{opp}} = \frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

Addition Formulas

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \sin \beta \cos \alpha$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\tan(\alpha + \beta) = \frac{\sin(\alpha + \beta)}{\cos(\alpha + \beta)} = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}$$

Subtraction Formulas

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \sin \beta \cos \alpha$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\tan(\alpha - \beta) = \frac{\sin(\alpha - \beta)}{\cos(\alpha - \beta)} = \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta}$$

Half-Angle Formulas

$$\sin\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$$

$$\cos\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$$

$$\tan\left(\frac{\alpha}{2}\right) = \frac{1 - \cos \alpha}{\sin \alpha} = \frac{\sin \alpha}{1 + \cos \alpha}$$

Double Angle Formulas

$$\sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$$

$$= 1 - 2 \sin^2 \alpha$$

$$= 2 \cos^2 \alpha - 1$$

$$\tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha}$$

Law of Sines

$$\frac{\sin \alpha}{a} = \frac{\sin \beta}{b} = \frac{\sin \gamma}{c}$$

Law of Cosines

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

$$b^2 = a^2 + c^2 - 2ac \cos \beta$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

Circular Sector

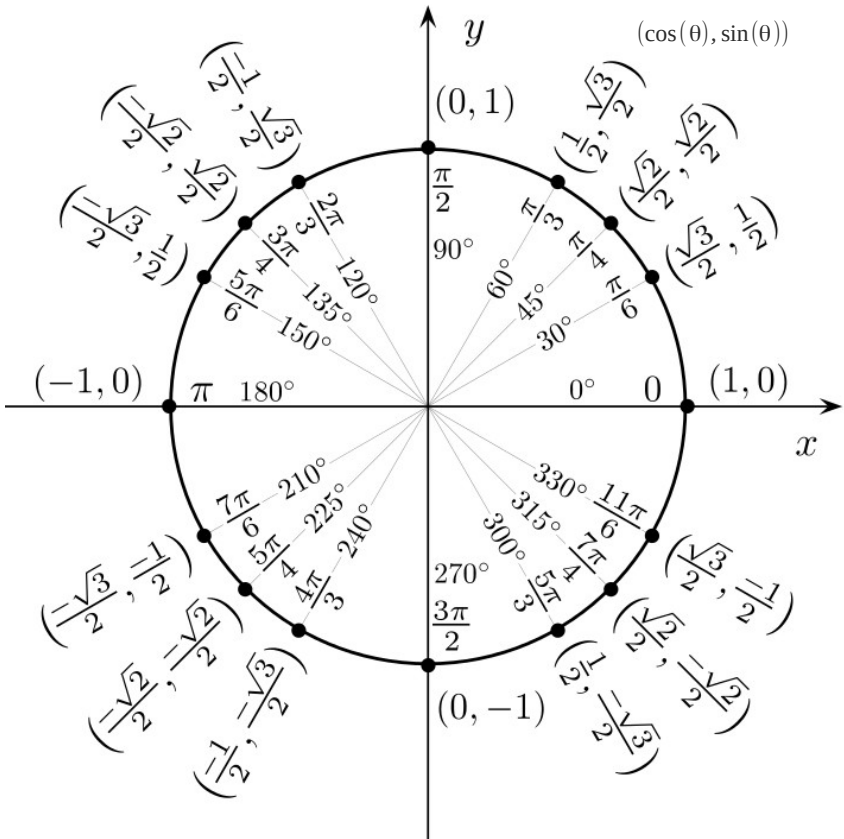
$$s = r\theta \quad A = \frac{1}{2}r^2\theta$$

Constants

$$\pi = 3.141592653589793238462643$$

$$e = 2.718281828459045235360287$$

$$\varphi = 1.618033988749894848204586$$



Formulas From Algebra

Quadratic Formula

if $ax^2 + bx + c = 0$ then

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\text{vertex} = \left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right) \right) = (h, k)$$

$$y = a(x - h)^2 + k$$

Distance Formula

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Midpoint Formula

$$\text{midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Factoring Formulas

$$x^2 - y^2 = (x + y)(x - y)$$

$$x^2 \pm 2xy + y^2 = (x \pm y)^2$$

$$x^3 \pm y^3 = (x \pm y)(x^2 \mp xy + y^2)$$

Associative Property

$$a + (b + c) = (a + b) + c$$

$$a(bc) = (ab)c$$

Commutative Property

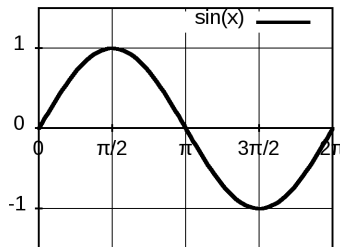
$$a + b = b + a$$

$$ab = ba$$

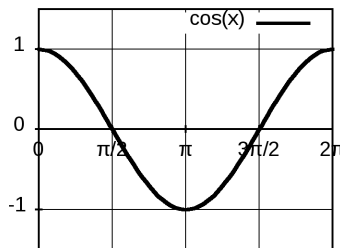
Distributive Property

$$a(b + c) = ab + ac$$

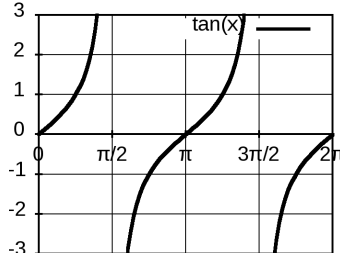
Sine Graph



Cosine Graph



Tangent Graph



Exponents and Radicals

$$a^x * a^y = a^{x+y}$$

$$(a^x)^y = a^{xy}$$

$$(ab)^x = a^x b^x$$

$$\left(\frac{a}{b}\right)^x = \frac{a^x}{b^x}$$

$$\frac{a^x}{a^y} = a^{x-y}$$

$$a^{-x} = \frac{1}{a^x}$$

$$a^{\frac{1}{x}} = \sqrt[x]{a}$$

$$\sqrt[x]{a^y} = a^{\frac{y}{x}}$$

Line Equations

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$y = m x + b$$

$$y - y_1 = m(x - x_1)$$

Circle Equations

Center = (h, k) radius = r :

$$(x-h)^2 + (y-k)^2 = r^2$$

$$y = k \pm \sqrt{r^2 - (x-h)^2}$$

Exponentials and Logarithms

$$y = \log_b x \Leftrightarrow b^y = x$$

$$\log(x y) = \log(x) + \log(y)$$

$$\log\left(\frac{x}{y}\right) = \log x - \log y$$

$$\log(x^a) = a \log(x)$$

$$a^{\log_a(x)} = x$$

$$\log_a(a^x) = x$$

$$\log(1) = 0$$

$$\log_a(a) = 1 \quad \ln(e) = 1$$

$$\log(x) = \log_{10}(x)$$

$$\ln(x) = \log_e(x)$$

$$\log_b(x) = \frac{\log(x)}{\log(b)} = \frac{\ln(x)}{\ln(b)}$$

Function Modifications

$$g(x) = a * f(b * x - c) + d$$

a = vertical stretch

b = horizontal squeeze

c = horizontal shift

d = vertical shift

Formulas from Geometry

Right Triangle

$$c^2 = a^2 + b^2 \quad A = \frac{1}{2} ab$$

Equilateral Triangle

$$h = \frac{\sqrt{3}}{2} s \quad A = \frac{\sqrt{3}}{4} s^2$$

Triangle

$$A = \frac{1}{2} bh = \frac{1}{2} ab \sin(\theta)$$

Trapezoid

$$A = \frac{1}{2}(a+b)h$$

Rectangle

$$A = l w \quad P = 2l + 2w$$

Circle

$$A = \pi r^2 \quad C = 2 \pi r$$

Right Circular Cone

$$V = \frac{1}{3} \pi r^2 h = \frac{1}{3} A_{base} h$$

$$S = \pi r \sqrt{r^2 + h^2}$$

Sphere

$$V = \frac{4}{3} \pi r^3 \quad S = 4 \pi r^2$$

Rectangular Box

$$V = l w h$$

$$S = 2hl + 2lw + 2hw$$

Right Circular Cylinder

$$V = \pi r^2 h$$

$$S = 2\pi r h + 2\pi r^2$$

Circular Sector

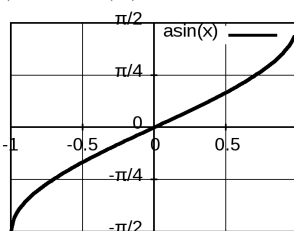
$$s = r\theta \quad A = \frac{1}{2} r^2 \theta$$

Parallelogram

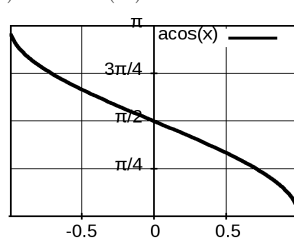
$$A = bh = ab \sin(\theta)$$

Inverse Trigonometry Functions

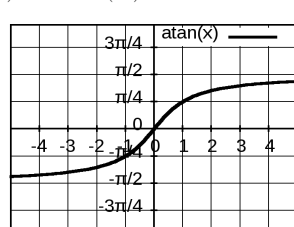
$$f(x) = \arcsin(x)$$



$$f(x) = \arccos(x)$$

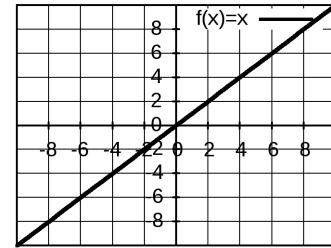


$$f(x) = \arctan(x)$$

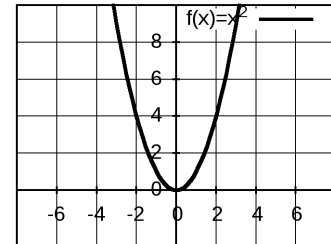


Common Function Graphs

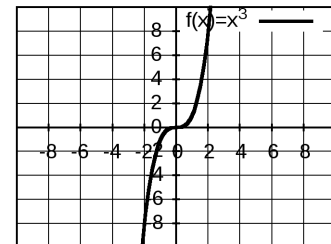
$$f(x) = x$$



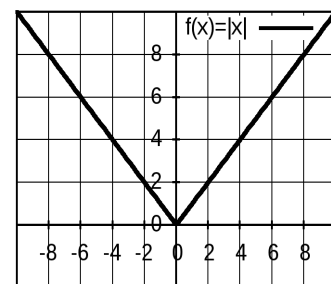
$$f(x) = x^2$$



$$f(x) = x^3$$



$$f(x) = |x|$$



$$f(x) = \sqrt{x}$$

